

CBSE Class 09 Mathematics

Revision Notes

CHAPTER – 2

POLYNOMIALS

1. Polynomials in one Variable
2. Zeroes of a Polynomial
3. Remainder Theorem
4. Factorisation of Polynomials
5. Algebraic Identities

Constants : A symbol having a fixed numerical value is called a constant.

Variables : A symbol which may be assigned different numerical values is known as variable.

Algebraic expressions : A combination of constants and variables connected by some or all of the operations $+$, $-$, $*$, $/$ is known as algebraic expression.

Terms : The several parts of an algebraic expression separated by '+' or '-' operations are called the terms of the expression.

Polynomials : An algebraic expression in which the variables involved have only non-negative integral powers is called a polynomial.

(i) $5x^2 - 4x^2 - 6x - 3$ is a polynomial in variable x .

(ii) $5 + 8x^{\frac{3}{2}} + 4x^{-2}$ is an expression but not a polynomial.

Polynomials are denoted by $p(x)$, $q(x)$ and $r(x)$ etc.

Coefficients : In the polynomial $x^3 + 3x^2 + 3x + 1$, coefficient of x^3 , x^2 , x are 1, 3, 3 respectively and we also say that +1 is the constant term in it.

Degree of a polynomial in one variable: In case of a polynomial in one variable the highest power of the variable is called the degree of the polynomial.

A polynomial of degree n has n roots.

Classification of polynomials on the basis of degree.

degree	Polynomial	Example
(a) 1	Linear	$x + 1, 2x + 3$ etc.
(b) 2	Quadratic	$ax^2 + bx + c$ etc.
(c) 3	Cubic	$x^3 + 3x^2 + 1$ etc.
(d) 4	Biquadratic	$x^4 - 1$

Classification of polynomials on the basis of number of terms

No. of terms	Polynomial & Examples.
(i) 1	Monomial - $5, 3x, \frac{1}{3}y$ etc.
(ii) 2	Binomial - $(3 + 6x), (x - 5y)$ etc.
(iii) 3	Trinomial- $2x^2 + 4x + 2$ etc.

Constant polynomial : A polynomial containing one term only, consisting a constant term is called a constant polynomial. The degree of non-zero constant polynomial is zero.

Zero polynomial : A polynomial consisting of one term, namely zero only is called a zero polynomial.

The degree of zero polynomial is not defined.

Zeros of a polynomial : Let $p(x)$ be a polynomial. If $p(a) = 0$, then we say that " a " is a zero of the polynomial of $p(x)$.

Remark : Finding the zeroes of polynomial $p(x)$ means solving the equation $p(x) = 0$.

Remainder theorem : Let $f(x)$ be a polynomial of degree $n \geq 1$ and let a be any real number. When $f(x)$ is divided by $(x - a)$ then the remainder is $f(a)$

Factor theorem : Let $f(x)$ be a polynomial of degree $n > 1$ and let a be any real number.

If $f(a) = 0$ then, $(x - a)$ is factor of $f(x)$

If $f(x - a)$ is factor of $f(x)$ then $f(a) = 0$

Factor : A polynomial $p(x)$ is called factor of $q(x)$ divides $q(x)$ exactly.

Factorization : To express a given polynomial as the product of polynomials each of degree less than that of the given polynomial such that no such a factor has a factor of lower degree, is called factorization.

Some algebraic identities useful in factorization:

$$(i) (x + y)^2 = (x)^2 + 2xy + (y)^2$$

$$(ii) (x - y)^2 = (x)^2 - 2xy + (y)^2$$

$$(iii) x^2 - y^2 = (x - y)(x + y)$$

$$(iv) (x + a)(x + b) = (x)^2 + (a + b)x + ab$$

$$(v) (x + y + z)^2 = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx$$

$$(vi) (x + y)^3 = x^3 + y^3 + 3xy(x + y)$$

$$(vii) (x - y)^3 = x^3 - y^3 - 3xy(x - y)$$

$$(viii) x^3 + y^3 + z^3 - 3xyz = (x + y + z) (x^2 + y^2 + z^2 - xy - yz - zx)$$

$$x^3 + y^3 + z^3 = 3xyz \text{ if } x + y + z = 0$$

$$(ix) a^3 + b^3 = (a + b) (a^2 - ab + b^2)$$

$$(x) a^3 - b^3 = (a - b) (a^2 + ab + b^2)$$